

# Quantum Computing

Jonathan A. Jones

## A Physical Systems: NMR

1. Estimate the strength of the magnetic field gradient required to make two  $^1\text{H}$  nuclei in a molecule (assume a separation of about  $1 \text{ \AA}$ ) have Larmor frequencies differing by about 100 Hz. Would it be possible to obtain a gradient of this size?
2. Show that a Heisenberg coupling in a two spin system can be approximated by an Ising coupling as long as  $|\omega_{12}| \ll |\omega_1 - \omega_2|$ .
3. Draw an explicit network of gates to implement a controlled-NOT gate in a two spin system, using only standard single qubit gates and the gate  $U(t)$  which corresponds to free evolution under the system's Hamiltonian for a time  $t$ . Draw an implementation of a NOT gate that takes the same length of time. (You may find it helpful to look back at section D of the Michaelmas Term problem sheet.)
4. Consider a system of three coupled spins. Write down the Hamiltonian and then design a spin echo sequence such that the average Hamiltonian is reduced to a single coupling term between the second and third spins.
5. Return to a one spin system, and design a spin echo style sequence which will reduce the spin's apparent Larmor frequency to one half of its true value. Is it possible to change the sign of a spin's apparent Larmor frequency? What are the limits on the possible range of scalings? Can coupling strengths be rescaled in the same way?